

POP

Errors:  $u_i$

SAMPLE

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Residuals:  $\hat{u}_i$

$$(\hat{u}_i = Y_i - (\hat{\beta}_0 + \hat{\beta}_1 X_{1,i} + \hat{\beta}_2 X_{2,i} \dots))$$

How do we get  $\hat{\beta}_k$ ?

$$(\hat{\beta}_0, \hat{\beta}_1, \dots) = \underset{(\beta_0, \beta_1, \dots)}{\operatorname{argmin}} \sum_{i=1}^n (Y_i - (\beta_0 + \beta_1 X_{1,i} + \beta_2 X_{2,i} \dots))^2$$

We find these by taking the first derivative of this objective function for each beta, and solving the system of equations, where each FD is set to  $= 0$ .

$$\min_{(\beta_0, \beta_1)} (Y_i - \beta_0 - \beta_1 X_i)^2$$

First Deriv. with respect to  $\beta_0$  set to 0:

$$\sum_{i=1}^n 2(Y_i - \hat{\beta}_0 - \hat{\beta}_1 X_i)(-1) = 0 \quad (1)$$

" " " "  $\beta_1$  " "

$$\sum_{i=1}^n 2(Y_i - \hat{\beta}_0 - \hat{\beta}_1 X_i)(-X_i) = 0 \quad (2)$$

Solving this system gives you

$\hat{\beta}_0, \hat{\beta}_1, \dots$  that we call OLS estimators.